

PRACTICE: Exponential and Logarithmic Functions

NO CALCULATORS

1. Solve each of the following for x .

a) $\log_2 \frac{1}{256} = x$

b) $\log_x 32 = -5$

c) $\log_5 \sqrt[3]{5} = x$

d) $\log_4 512 = x$

e) $\log_x 36 = -2$

f) $\log_x \sqrt{\frac{4}{9}} = \frac{1}{2}$

2. Solve each of the following for x .

a) $\left(\frac{2}{3}\right)^{x-1} + \left(\frac{2}{3}\right)^x = \frac{20}{27}$

b) $2^{x+2} - 2^x = 96$

c) $4^{x-1} + 4^{x-3} = 272$

d) $\left(\frac{1}{2}\right)^{x-2} - \left(\frac{1}{2}\right)^x = \frac{3}{32}$

3. Solve each equation for x .

a) $\log_2(4x - 3) = \log_2\left(\frac{1}{2}x + 2\right)$

b) $\log_3(3x) = \log_3(8x - 10)$

c) $\log_4(-\frac{4}{5}x) = \log_4\left(-x - \frac{9}{5}\right)$

d) $\log(11 - x) = \log(1 - 2x)$

4. Solve each equation for x .

a) $\log x + \log x^2 = 3$

b) $\log_4 x^2 - \log_4 x = 2$

c) $\log_{12} x^3 - \log_{12} x^5 = -2$

d) $\log_3 x^4 + \log_3 x = 5$

5. Solve each of the following for x .

a) $\log_6(x + 1) + \log_6(x + 2) = 1$

b) $\log_7(x + 2) + \log_7(x - 4) = 1$

c) $\log_2(x + 2) = 3 - \log_2 x$

d) $\log_4 x + \log_4(x + 6) = 2$

e) $\log_5(2x + 2) - \log_5(x - 1) = \log_5(x + 1)$

f) $9^{x+1} = 27^{2x}$

6. Solve each of the following for x .

a) $\log_5 x = 3$

b) $\log_4 x = 2$

c) $\log_x 27 = 3$

d) $\log_4\left(\frac{1}{64}\right) = x$

e) $\log_x\left(\frac{1}{9}\right) = 2$

f) $\log_{\frac{1}{4}} x = -2$

7. Evaluate.

a) $\log_2 16^{-2}$

b) $2^{\log_2 20}$

c) $\log_3 \frac{1}{27}$

d) $\log_6 72 - \log_6 2$

e) $\log_3 0.9 + \log_3 10$

f) $\log_6 216^5$

Answers

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|----------------------|------------------|------------------|--------|------------------|------------------|
| 1. a) -8 | b) $\frac{1}{2}$ | c) $\frac{1}{3}$ | d) 4.5 | e) $\frac{1}{6}$ | f) $\frac{4}{9}$ |
| 2. a) 3 | b) 5 | c) 5 | d) 5 | | |
| 3. a) $\frac{10}{7}$ | b) 2 | c) -9 | d) -10 | | |
| 4. a) 10 | b) 16 | c) 12 | d) 3 | | |
| 5. a) 1 | b) 5 | c) 2 | d) 2 | e) 3 | f) $\frac{1}{2}$ |
| 6. a) 125 | b) 16 | c) 3 | d) -3 | e) $\frac{1}{3}$ | f) 16 |
| 7. a) -8 | b) 20 | c) -3 | d) 2 | e) 2 | f) 15 |