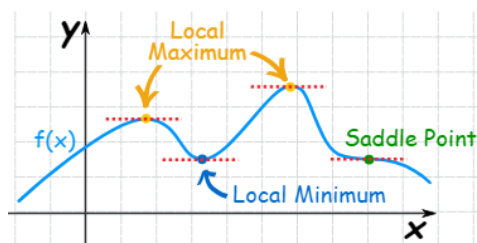


## Lesson 2.05: Solving Problems Involving Rates of Change



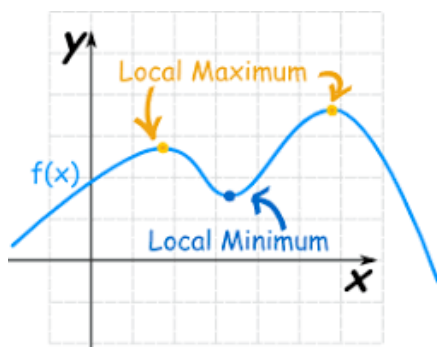
### Learning Goals:

- I know what a global maximum and a global minimum is;
- I know what a local maximum and a local minimum is;
- I know when it is required to calculate a rate of change;
- I can calculate the exact rate of change.



## Local Maximum or Minimum

Given  $y = f(x)$ . For values of  $x$  near  $c$  ...



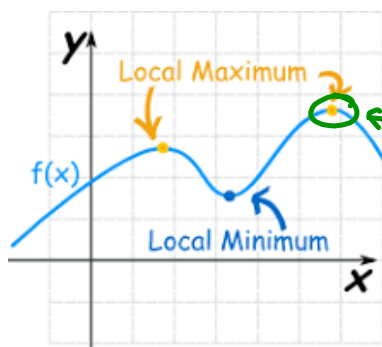
A local maximum at  $x = c$  exists if the function's rate of change changes from positive to negative through  $x = c$ .

A local minimum at  $x = c$  exists if the function's rate of change changes from negative to positive through  $x = c$ .

In both cases, at  $x = c$  the rate of change will be zero (or undefined).

## Global Maximum or Minimum

Given  $y = f(x)$ ...



A global maximum at  $x = c$  exists if  $f(c) > f(x)$  for all values of  $x$  in the function's domain.

A global minimum at  $x = c$  exists if  $f(c) < f(x)$  for all values of  $x$  in the function's domain.

## Example 1

Using the First Principles Difference Quotient, prove that a local minimum value occurs at  $x = 3$  for the function  $f(x) = x^2 - 6x + 5$ . Verify graphically.

$$\begin{aligned} & \frac{f(x+h) - f(x)}{h}, h \rightarrow 0 \\ | & = \frac{(x+h)^2 - 6(x+h) + 5 - [x^2 - 6x + 5]}{h}, h \rightarrow 0 \\ & = \frac{\cancel{x^2} + 2xh + h^2 - \cancel{6x} - 6h + \cancel{5} - \cancel{x^2} + \cancel{6x} - \cancel{5}}{h}, h \rightarrow 0 \\ & = \frac{h^2 + 2xh - 6h}{h}, h \rightarrow 0 \\ & = \frac{h(h + 2x - 6)}{h}, h \rightarrow 0 \\ & = h + 2x - 6, h \rightarrow 0 \\ & = 2x - 6 \end{aligned}$$

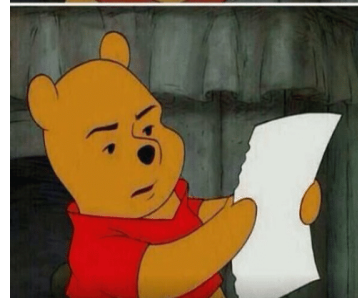
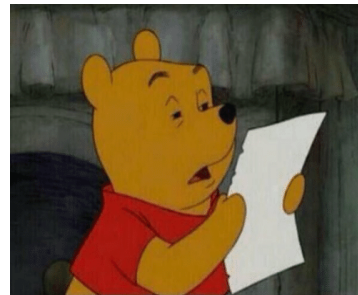
$x < 3$	$x = 3$	$x > 3$
$2(2.9) - 6$	$2(3) - 6$	$2(3.1) - 6$
$= 5.8 - 6$	$= 6 - 6$	$= 6.2 - 6$
$= -0.2$	$= 0$	$= 0.2$

$$f(x) = \cos x$$

$$\begin{aligned} & \frac{f(180+h) - f(180)}{h} \\ & = \frac{\cos(180+h) - \cos(180)}{h} \end{aligned}$$

## Homework

Use the First Principles Difference Quotient for all  
Rate of Change calculations  
pg. 111-113 #1, 3, 4, 6c, 9a, 10, 14



Staring at my math homework  
like